Exercise 3

For the following exercises, determine whether the relation is a function.

 $y^2 + 4 = x$, for x the independent variable and y the dependent variable

Solution

Solve the given equation for y.

$$y^2 = x - 4$$

Take the square root of both sides.

$$\sqrt{y^2} = \sqrt{x-4}$$

Since there's an even power under an even root and the result is to an odd power, an absolute sign is needed.

$$|y| = \sqrt{x - 4}$$

Remove the absolute value sign by placing \pm on the right side.

$$y = \pm \sqrt{x - 4}$$

The relation is not a function because for any given input x, there are two corresponding outputs, $y = \sqrt{x-4}$ and $y = -\sqrt{x-4}$.